### Basic Data Structures: Stacks and Queues

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Data Structures Data Structures and Algorithms

### Outline





Stack: Abstract data type with the following operations:

Push(Key): adds key to collection

- Push(Key): adds key to collection
- Key Top(): returns most recently-added key

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- Key Top(): returns most recently-added key
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- Key Top(): returns most recently-added key
- Key Pop(): removes and returns most recently-added key
- Boolean Empty(): are there any elements?

#### Balanced Brackets

# Input: A string *str* consisting of '(', ')', '[', ']' characters.

# Output: Return whether or not the string's parentheses and square brackets are balanced.

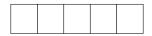
#### Balanced Brackets

Balanced:

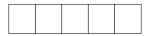
"([])[]()",
"((([[])]))())"
Unbalanced:

#### IsBalanced(str)

```
Stack stack
for char in str:
  if char in ['(', '[']:
    stack.Push(char)
  else:
    if stack.Empty(): return False
    top \leftarrow stack.Pop()
    if (top = '[' and char != ']') or
       (top = `(` and char != `)`):
      return False
return stack.Empty()
```

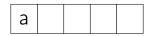


#### numElements: 0

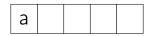


Push(a)

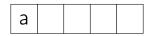
#### numElements: 1



#### Push(a)



#### numElements: 1

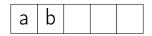


#### Push(b)

#### numElements: 2



#### Push(b)



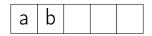
#### numElements: 2



Top()



 $Top() \rightarrow b$ 



#### numElements: 2



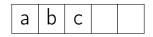
#### Push(c)

#### numElements: 3

#### Push(c)



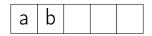
#### numElements: 3



Pop()



 $Pop() \rightarrow c$ 

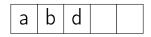


#### numElements: 2

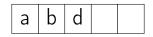


#### Push(d)

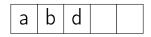
#### numElements: 3



#### Push(d)



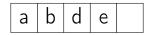
#### numElements: 3



#### Push(e)

#### numElements: 4

#### Push(e)



#### numElements: 4

#### Push(f)

#### numElements: 5

#### Push(f)

#### numElements: 5

Push(g)

### numElements: 5

#### $Push(g) \rightarrow ERROR$

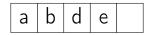
### numElements: 5

#### $Empty() \rightarrow False$

### numElements: 5

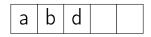
Pop()

$$Pop() \rightarrow f$$

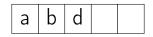


#### numElements: 4

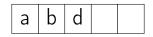
Pop()



$$Pop() \rightarrow e$$



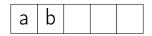
### numElements: 3



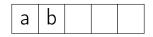
Pop()



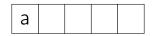
$$Pop() \rightarrow d$$



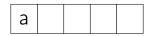
#### numElements: 2



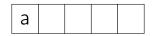
Pop()



 $Pop() \rightarrow b$ 



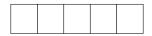
### numElements: 1



Pop()



 $Pop() \rightarrow a$ 

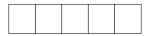


#### numElements: 0

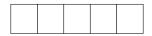


Empty()

#### numElements: 0



Empty()  $\rightarrow$  True







Push(a)



#### Push(a)





#### Push(b)



#### Push(b)





#### Top()

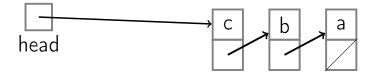


 $Top() \rightarrow b$ 

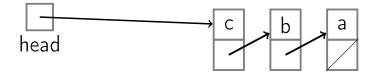


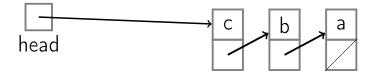


#### Push(c)



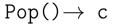
#### Push(c)





Pop()

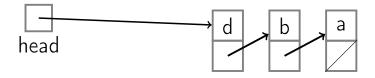




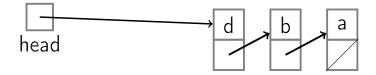


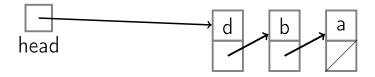


#### Push(d)

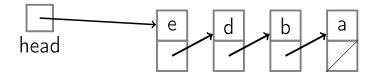


#### Push(d)

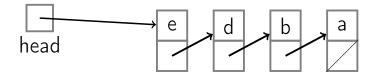


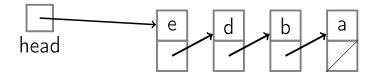


#### Push(e)

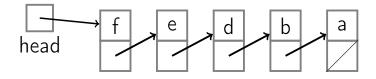


#### Push(e)

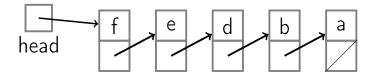


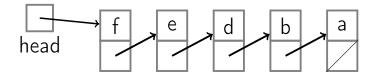


#### Push(f)

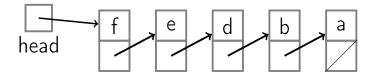


Push(f)

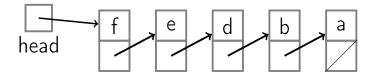


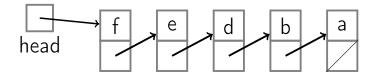


#### Empty()

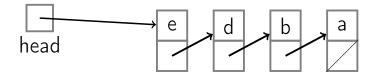


 $Empty() \rightarrow False$ 

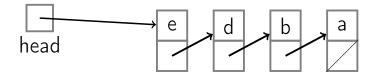


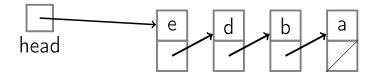


Pop()

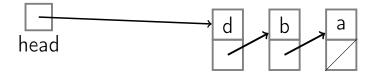


 $Pop() \rightarrow f$ 

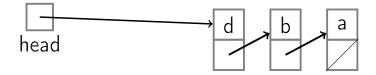


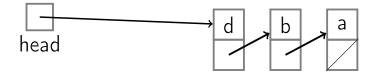


#### Pop()



#### $Pop() \rightarrow e$





#### Pop()



#### $Pop() \rightarrow d$





#### Pop()



#### $Pop() \rightarrow b$





#### Pop()



 $Pop() \rightarrow a$ 





Empty()



 $Empty() \rightarrow True$ 



#### Summary

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- Each stack operation is O(1): Push, Pop, Top, Empty.
- Stacks are ocassionaly known as LIFO queues.

#### Outline





# Queue: Abstract data type with the following operations:

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Enqueue(Key): adds key to collection

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#### FIFO: First-In, First-Out

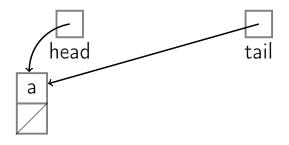




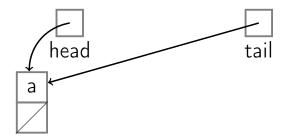


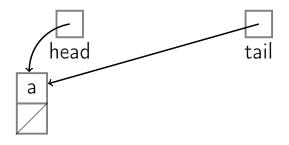


#### Enqueue(a)

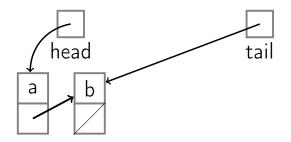


Enqueue(a)

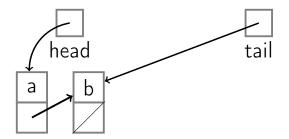


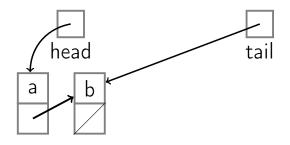


Enqueue(b)

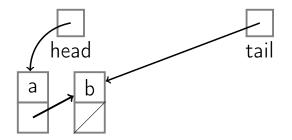


#### Enqueue(b)

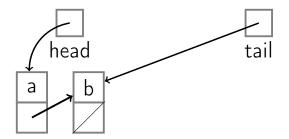


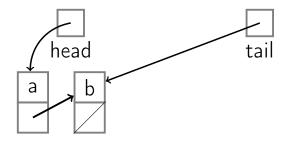


Empty()

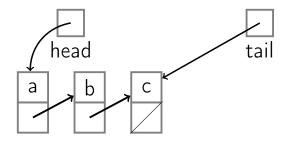


 $Empty() \rightarrow False$ 

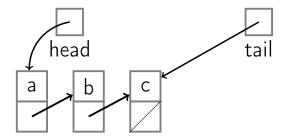


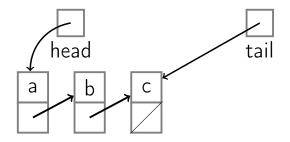


Enqueue(c)

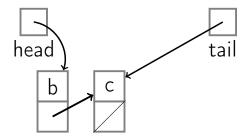


Enqueue(c)

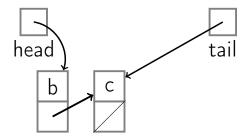


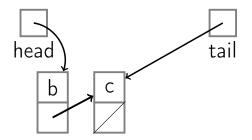


Dequeue()

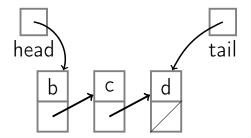


$$ext{Dequeue}( ext{)} 
ightarrow$$
 a

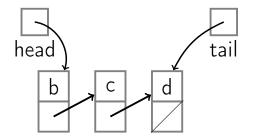


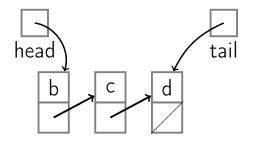


Enqueue(d)

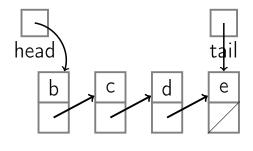


Enqueue(d)

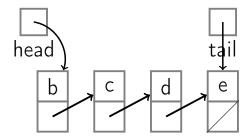


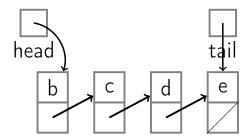


Enqueue(e)

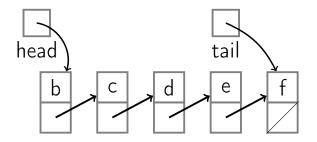


Enqueue(e)

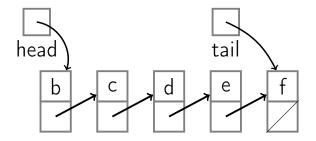


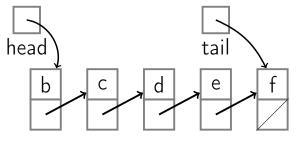


Enqueue(f)

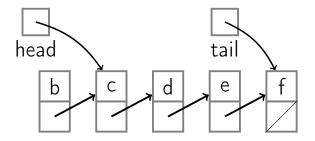


Enqueue(f)

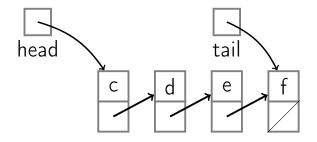


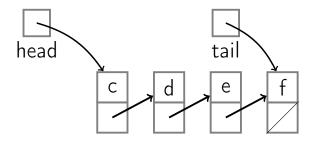


Dequeue()

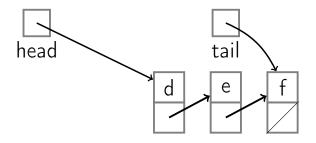


 $Dequeue() \rightarrow b$ 

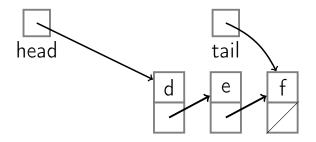


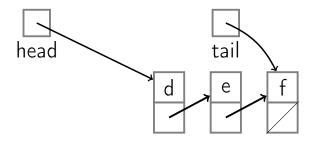


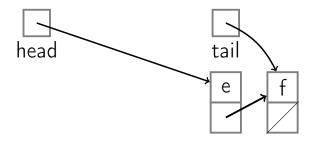
Dequeue()



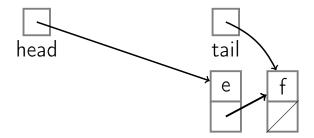
Dequeue()  $\rightarrow$  c

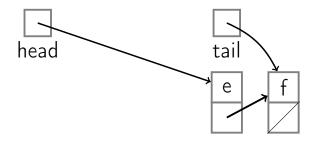




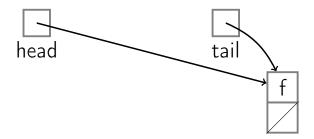


#### $Dequeue() \rightarrow d$

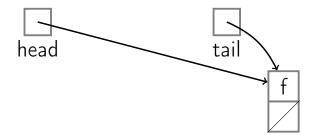


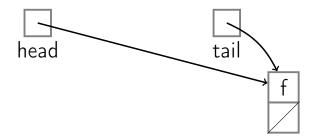


Dequeue()



Dequeue()
$$\rightarrow$$
 e





Dequeue()





Dequeue() 
$$\rightarrow$$
 f













Empty() 
$$\rightarrow$$
 True

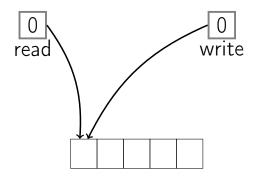


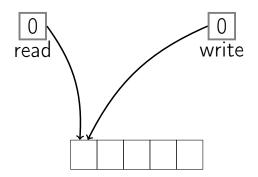


#### Enqueue: use List.PushBack

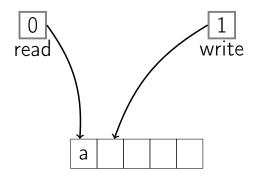
 Enqueue: use List.PushBack
 Dequeue: use List.TopFront and List.PopFront

- Enqueue: use List.PushBack
- Dequeue: use List.TopFront and List.PopFront
- Empty: use List.Empty

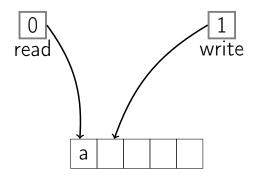


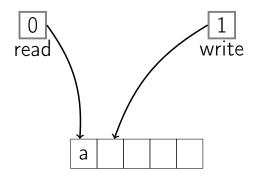


Enqueue(a)

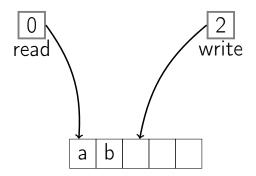


Enqueue(a)

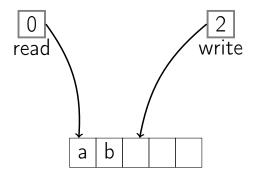


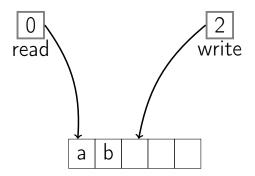


Enqueue(b)

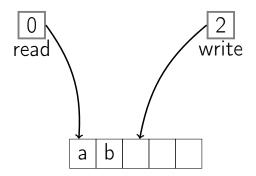


Enqueue(b)

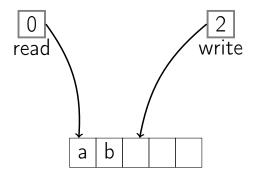


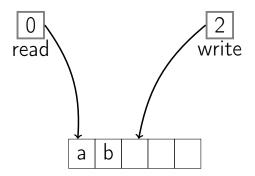


Empty()

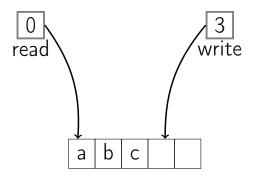


 $Empty() \rightarrow False$ 

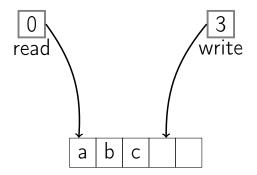


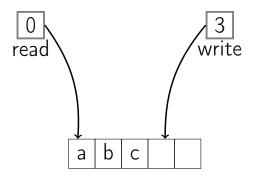


Enqueue(c)

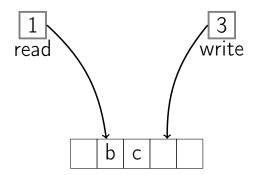


Enqueue(c)

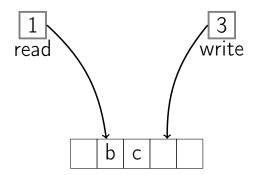


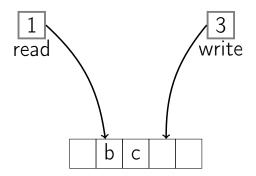


Dequeue()

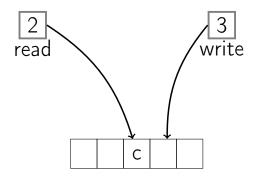


 $Dequeue() \rightarrow a$ 

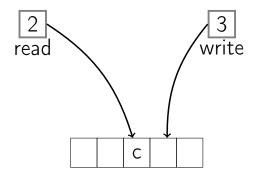


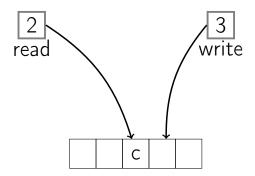


Dequeue()

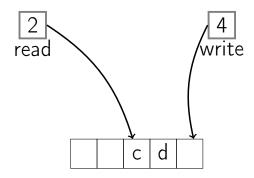


Dequeue()  $\rightarrow$  b

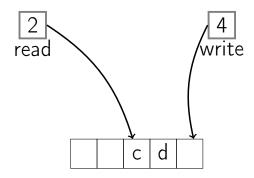


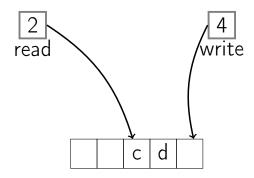


Enqueue(d)

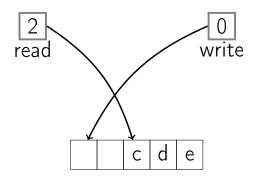


Enqueue(d)

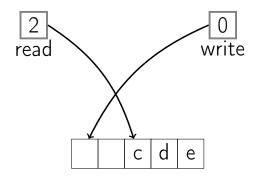


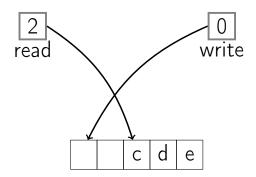


Enqueue(e)

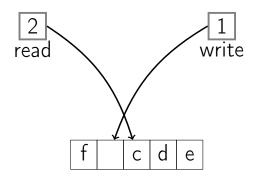


Enqueue(e)

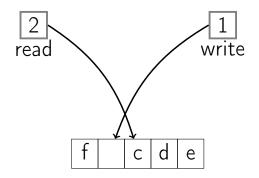


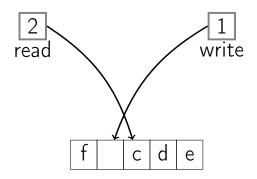


Enqueue(f)

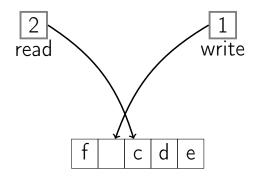


Enqueue(f)

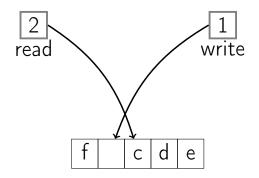


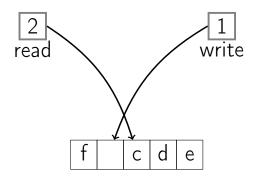


Enqueue(g)

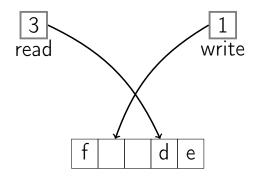


 $Enqueue(g) \rightarrow ERROR$ 

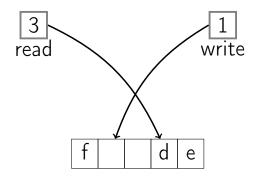


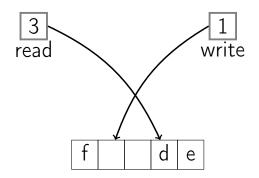


Dequeue()

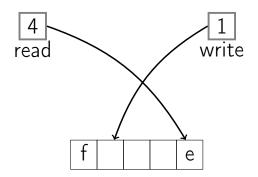


Dequeue()  $\rightarrow$  c

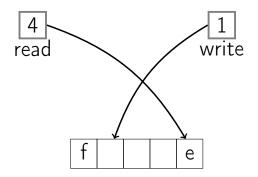


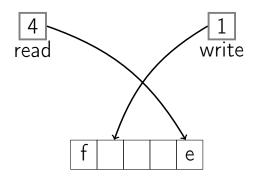


Dequeue()

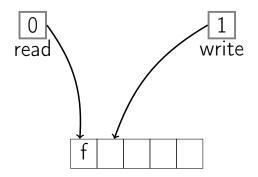


Dequeue()  $\rightarrow$  d

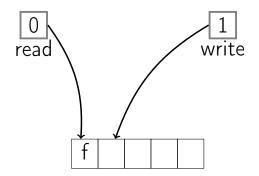


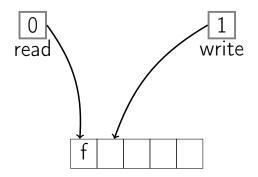


Dequeue()

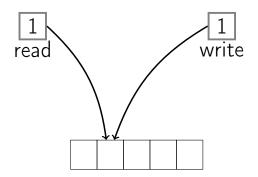


 $Dequeue() \rightarrow e$ 

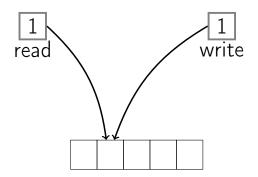


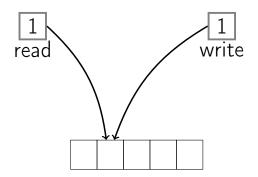


Dequeue()

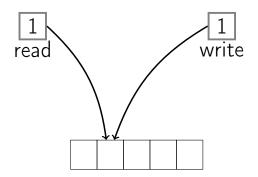


 $Dequeue() \rightarrow f$ 





Empty()



 $Empty() \rightarrow True$ 

# Summary

#### Summary

#### Queues can be implemented with either a linked list (with tail pointer) or an array.

# Summary

- Queues can be implemented with either a linked list (with tail pointer) or an array.
- Each queue operation is O(1): Enqueue, Dequeue, Empty.