# Basic Data Structures: Stacks and Queues 

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## Data Structures <br> Data Structures and Algorithms

## Outline

(1) Stacks
(2) Queues

## Definition

Stack: Abstract data type with the following operations:

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\author{

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- Key Pop(): removes and returns most recently-added key


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■ Push(Key): adds key to collection

- Key Top(): returns most recently-added key
- Key Pop(): removes and returns most recently-added key
■ Boolean Empty(): are there any elements?


## Balanced Brackets

Input: A string str consisting of '(', ')', '[', ']' characters.
Output: Return whether or not the string's parentheses and square brackets are balanced.

## Balanced Brackets

Balanced:

$$
\begin{aligned}
& \text { ■"([])[]()", } \\
& \text { " "((([([])]))())" }
\end{aligned}
$$

Unbalanced:

$$
\begin{aligned}
& \text { " " }[\text { []] ( )" } \\
& \text { "] }] \text { " }
\end{aligned}
$$

## IsBalanced(str)

Stack stack for char in str:
if char in ['(', '[']: stack.Push(char)
else:
if stack.Empty(): return False top $\leftarrow$ stack.Pop()
if (top = '[' and char != ']') or
(top = '(' and char != ')'):
return False
return stack.Empty()

## Stack Implementation with Array

numElements: 0


# Stack Implementation with Array 

numElements: 0


## Push (a)

# Stack Implementation with Array 

numElements: 1


## Push (a)

# Stack Implementation with Array 

numElements: 1


# Stack Implementation with Array 

numElements: 1


## Push (b)

# Stack Implementation with Array 

numElements: 2


## Push (b)

## Stack Implementation with Array

numElements: 2


# Stack Implementation with Array 

numElements: 2


## Top()

# Stack Implementation with Array 

numElements: 2


$$
\operatorname{Top}() \rightarrow b
$$

## Stack Implementation with Array

numElements: 2


# Stack Implementation with Array 

numElements: 2


## Push (c)

# Stack Implementation with Array 

numElements: 3


## Push (c)

# Stack Implementation with Array 

numElements: 3


# Stack Implementation with Array 

numElements: 3

Pop()

# Stack Implementation with Array 

numElements: 2

$\operatorname{Pop}() \rightarrow c$

## Stack Implementation with Array

numElements: 2


# Stack Implementation with Array 

numElements: 2


## Push (d)

# Stack Implementation with Array 

numElements: 3


## Push (d)

# Stack Implementation with Array 

numElements: 3


# Stack Implementation with Array 

numElements: 3


Push (e)

# Stack Implementation with Array 

numElements: 4


Push (e)

## Stack Implementation with Array

numElements: 4


# Stack Implementation with Array 

numElements: 4


Push (f)

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

Push (f)

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

## Push (g)

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

Push (g) $\rightarrow$ ERROR

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

Empty ()

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

Empty () $\rightarrow$ False

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

# Stack Implementation with Array 

numElements: 5

| $a$ | $b$ | $d$ | $e$ | $f$ |
| :--- | :--- | :--- | :--- | :--- |

## Pop()

# Stack Implementation with Array 

numElements: 4


Pop() $\rightarrow$ f

## Stack Implementation with Array

numElements: 4


# Stack Implementation with Array 

numElements: 4


## Pop()

# Stack Implementation with Array 

numElements: 3

$\operatorname{Pop}() \rightarrow e$

# Stack Implementation with Array 

numElements: 3


# Stack Implementation with Array 

numElements: 3


## Pop()

# Stack Implementation with Array 

numElements: 2


$$
\operatorname{Pop}() \rightarrow d
$$

## Stack Implementation with Array

numElements: 2


# Stack Implementation with Array 

numElements: 2


## Pop()

# Stack Implementation with Array 

numElements: 1


$$
\operatorname{Pop}() \rightarrow b
$$

# Stack Implementation with Array 

numElements: 1


# Stack Implementation with Array 

numElements: 1


## Pop()

# Stack Implementation with Array 

numElements: 0


$$
\operatorname{Pop}() \rightarrow \mathrm{a}
$$

## Stack Implementation with Array

numElements: 0


# Stack Implementation with Array 

numElements: 0


Empty ()

# Stack Implementation with Array 

numElements: 0


Empty () $\rightarrow$ True

## Stack Implementation with Array

numElements: 0


## Stack Implementation with Linked List



# Stack Implementation with Linked List 

Push (a)

## Stack Implementation with Linked List



Push (a)

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Push (b)

## Stack Implementation with Linked List



Push (b)

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Top ()

## Stack Implementation with Linked List


$\operatorname{Top}() \rightarrow b$

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Push (c)

# Stack Implementation with Linked List 



Push (c)

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Pop()

## Stack Implementation with Linked List



Pop() $\rightarrow$ c

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Push (d)

# Stack Implementation with Linked List 



Push (d)

## Stack Implementation with Linked List



# Stack Implementation with Linked List 



Push (e)

## Stack Implementation with Linked List



Push (e)

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Push (f)

## Stack Implementation with Linked List



Push (f)

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Empty ()

## Stack Implementation with Linked List



Empty () $\rightarrow$ False

## Stack Implementation with Linked List



## Stack Implementation with Linked List


Pop()

## Stack Implementation with Linked List


$\operatorname{Pop}() \rightarrow f$

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Pop()

## Stack Implementation with Linked List


$\operatorname{Pop}() \rightarrow e$

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Pop()

## Stack Implementation with Linked List


$\operatorname{Pop}() \rightarrow d$

## Stack Implementation with Linked List



## Stack Implementation with Linked List



Pop()

## Stack Implementation with Linked List


$\operatorname{Pop}() \rightarrow b$

## Stack Implementation with Linked List



## Stack Implementation with Linked List



## Pop()

# Stack Implementation with Linked List 

$\operatorname{Pop}() \rightarrow \mathrm{a}$

## Stack Implementation with Linked List



# Stack Implementation with Linked List 



Empty()

# Stack Implementation with Linked List 

Empty() $\rightarrow$ True

## Stack Implementation with Linked List



## Stack Implementation with Linked List

## Stack Implementation with Linked List

## Stack Implementation with Linked List

## Summary

- Stacks can be implemented with either an array or a linked list.


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- Each stack operation is $O(1)$ : Push, Pop, Top, Empty.


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■ Each stack operation is $O(1)$ : Push, Pop, Top, Empty.
- Stacks are ocassionaly known as LIFO queues.


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(2) Queues

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- Enqueue (Key): adds key to collection
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FIFO: First-In, First-Out

# Queue Implementation with Linked List 



# Queue Implementation with Linked List 



Enqueue (a)

# Queue Implementation with Linked List 



Enqueue (a)

## Queue Implementation with Linked List



# Queue Implementation with Linked List 



Enqueue (b)

## Queue Implementation with Linked List



Enqueue (b)

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Empty ()

## Queue Implementation with Linked List



Empty() $\rightarrow$ False

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Enqueue (c)

## Queue Implementation with Linked List



Enqueue (c)

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Dequeue()

## Queue Implementation with Linked List



Dequeue() $\rightarrow$ a

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Enqueue (d)

## Queue Implementation with Linked List



Enqueue (d)

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Enqueue(e)

## Queue Implementation with Linked List



Enqueue(e)

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Enqueue (f)

## Queue Implementation with Linked List



Enqueue (f)

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Dequeue()

## Queue Implementation with Linked List



Dequeue ()$\rightarrow b$

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Dequeue()

## Queue Implementation with Linked List



Dequeue() $\rightarrow c$

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Dequeue()

## Queue Implementation with Linked List



Dequeue() $\rightarrow \mathrm{d}$

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Dequeue()

## Queue Implementation with Linked List



Dequeue() $\rightarrow$ e

## Queue Implementation with Linked List



## Queue Implementation with Linked List



Dequeue()

# Queue Implementation with Linked List 



Dequeue() $\rightarrow$ f

# Queue Implementation with Linked List 



# Queue Implementation with Linked List 



Empty ()

# Queue Implementation with Linked List 



Empty() $\rightarrow$ True

# Queue Implementation with Linked List 



# Queue Implementation with Linked List 

■ Enqueue: use List.PushBack

# Queue Implementation with Linked List 

■ Enqueue: use List. PushBack
■ Dequeue: use List. TopFront and List. PopFront

# Queue Implementation with Linked List 

- Enqueue: use List. PushBack
- Dequeue: use List. TopFront and List. PopFront
■ Empty: use List.Empty


## Queue Implementation with Array



## Queue Implementation with Array



Enqueue(a)

## Queue Implementation with Array



## Enqueue(a)

## Queue Implementation with Array



## Queue Implementation with Array



Enqueue (b)

## Queue Implementation with Array



Enqueue (b)

## Queue Implementation with Array



## Queue Implementation with Array



Empty ()

## Queue Implementation with Array



Empty() $\rightarrow$ False

## Queue Implementation with Array



## Queue Implementation with Array



Enqueue (c)

## Queue Implementation with Array



Enqueue (c)

## Queue Implementation with Array



## Queue Implementation with Array



Dequeue()

## Queue Implementation with Array



Dequeue() $\rightarrow$ a

## Queue Implementation with Array



## Queue Implementation with Array



Dequeue()

## Queue Implementation with Array



Dequeue() $\rightarrow$ b

## Queue Implementation with Array



## Queue Implementation with Array



Enqueue (d)

## Queue Implementation with Array



Enqueue (d)

## Queue Implementation with Array



## Queue Implementation with Array



Enqueue (e)

## Queue Implementation with Array



Enqueue (e)

## Queue Implementation with Array



## Queue Implementation with Array



Enqueue (f)

## Queue Implementation with Array



Enqueue (f)

## Queue Implementation with Array



## Queue Implementation with Array



Enqueue (g)

## Queue Implementation with Array



Enqueue $(\mathrm{g}) \rightarrow$ ERROR

## Queue Implementation with Array



## Queue Implementation with Array



Dequeue()

## Queue Implementation with Array



Dequeue() $\rightarrow$ c

## Queue Implementation with Array



## Queue Implementation with Array



Dequeue()

## Queue Implementation with Array



Dequeue() $\rightarrow \mathrm{d}$

## Queue Implementation with Array



## Queue Implementation with Array



Dequeue()

## Queue Implementation with Array



Dequeue() $\rightarrow$ e

## Queue Implementation with Array



## Queue Implementation with Array



Dequeue()

## Queue Implementation with Array



Dequeue() $\rightarrow$ f

## Queue Implementation with Array



## Queue Implementation with Array



Empty ()

## Queue Implementation with Array



Empty() $\rightarrow$ True

## Summary

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- Each queue operation is $O(1)$ : Enqueue, Dequeue, Empty.

